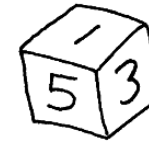


Roll a fair dice. Record the result.

$$X \sim \text{Uniform}(\{1,2,\dots,6\})$$



```
>> X = randi(6)
```

```
X =
```

```
5
```

Again, roll a fair dice. Record the result.

```
>> X = randi(6)
```

```
X =
```

```
6
```

Again, roll a fair dice. Record the result.

```
>> X = randi(6)
```

```
X =
```

```
1
```

Again, roll a fair dice. Record the result.

```
>> X = randi(6)
```

```
X =
```

```
6
```

Again, roll a fair dice. Record the result.

```
>> X = randi(6)
```

```
X =
```

```
4
```

Again, roll a fair dice. Record the result.

```
>> X = randi(6)
```

```
X =
```

```
1
```

```
>> X = randi(6,20,10)
```

```
X =
```

2	5	3	4	5	2	1	2	6	3
4	3	4	1	5	4	3	1	6	4
6	4	5	1	3	5	2	2	4	5
6	2	5	2	4	5	5	2	1	1
1	5	2	6	1	3	3	3	2	6
6	1	5	2	1	1	6	1	3	5
6	2	4	5	4	2	2	6	5	3
3	1	1	2	5	6	2	6	1	3
5	1	1	6	6	1	1	3	1	3
1	5	3	3	1	5	1	3	2	2
3	5	6	2	4	4	6	3	4	4
6	2	3	2	3	6	4	6	5	4
5	6	4	4	1	1	4	3	4	5
6	1	2	3	3	3	1	1	3	5
4	3	5	3	1	1	6	5	4	4
1	3	2	5	5	6	4	3	2	3
6	5	4	4	2	1	3	2	5	5
6	5	5	4	4	5	4	3	2	4
5	2	6	6	1	5	3	1	5	3
5	3	6	2	4	6	1	1	2	6

Generate X 200 times. Put the results in a table of size 20×10



randi function

- Generate uniformly distributed pseudorandom **integers**
- `randi(imax)` returns a scalar value between 1 and `imax`.
- `randi(imax, m, n)` and `randi(imax, [m, n])` return an *m*-by-*n* matrix containing pseudorandom integer values drawn from the discrete uniform distribution on the interval `[1, imax]`.
 - `randi(imax)` is the same as `randi(imax, 1)`.
- `randi([imin, imax], ...)` returns an array containing integer values drawn from the discrete uniform distribution on the interval `[imin, imax]`.

hist function

- Create histogram plot
- `hist(data)` creates a histogram bar plot of data.
 - Elements in data are sorted into **10 equally spaced bins** along the x-axis **between the minimum and maximum** values of data.
 - Bins are displayed as rectangles such that the height of each rectangle indicates the number of elements in the bin.
 - If data is a vector, then one histogram is created.
 - If data is a matrix, then a histogram is created separately for each column.
 - Each histogram plot is displayed on the same figure with a different color.
- `hist(data, nbins)` sorts data into the number of bins specified by `nbins`.
- `hist(data, xcenters)`
 - The values in `xcenters` **specify the centers** for each bin on the x-axis.

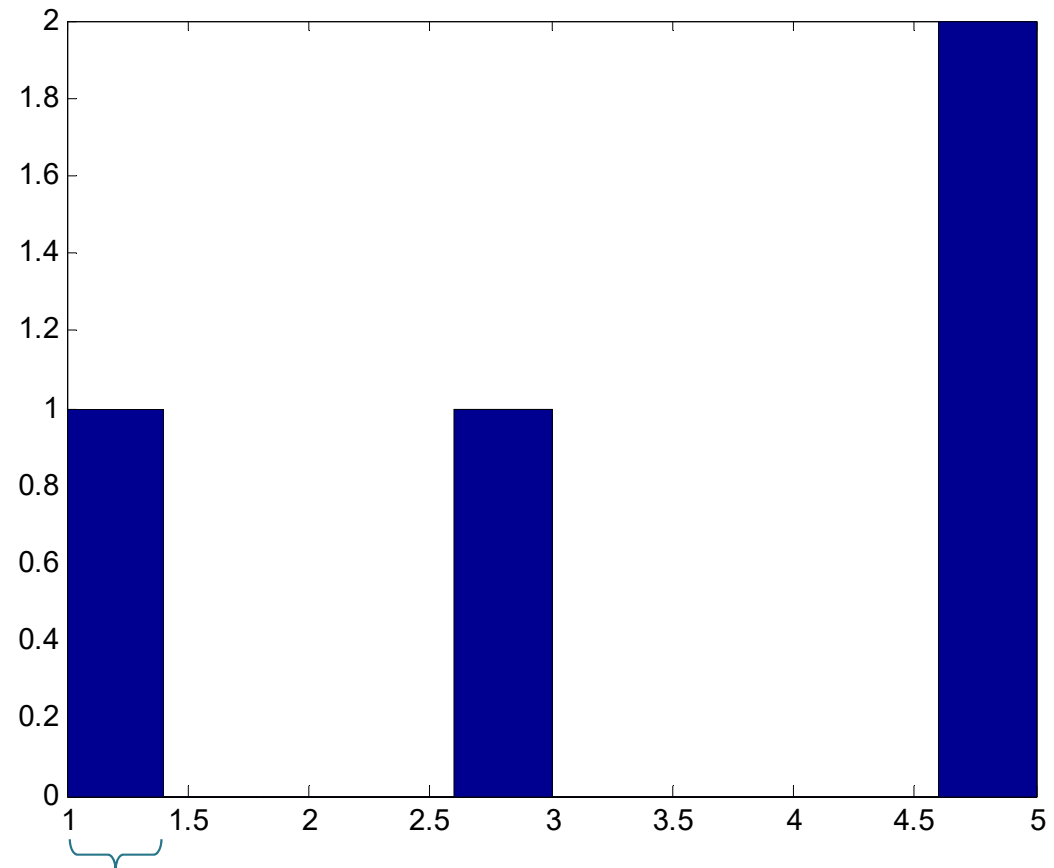
hist function: Example

```
>> x = [1 3 5 5]
```

```
x =
```

```
     1     3     5     5
```

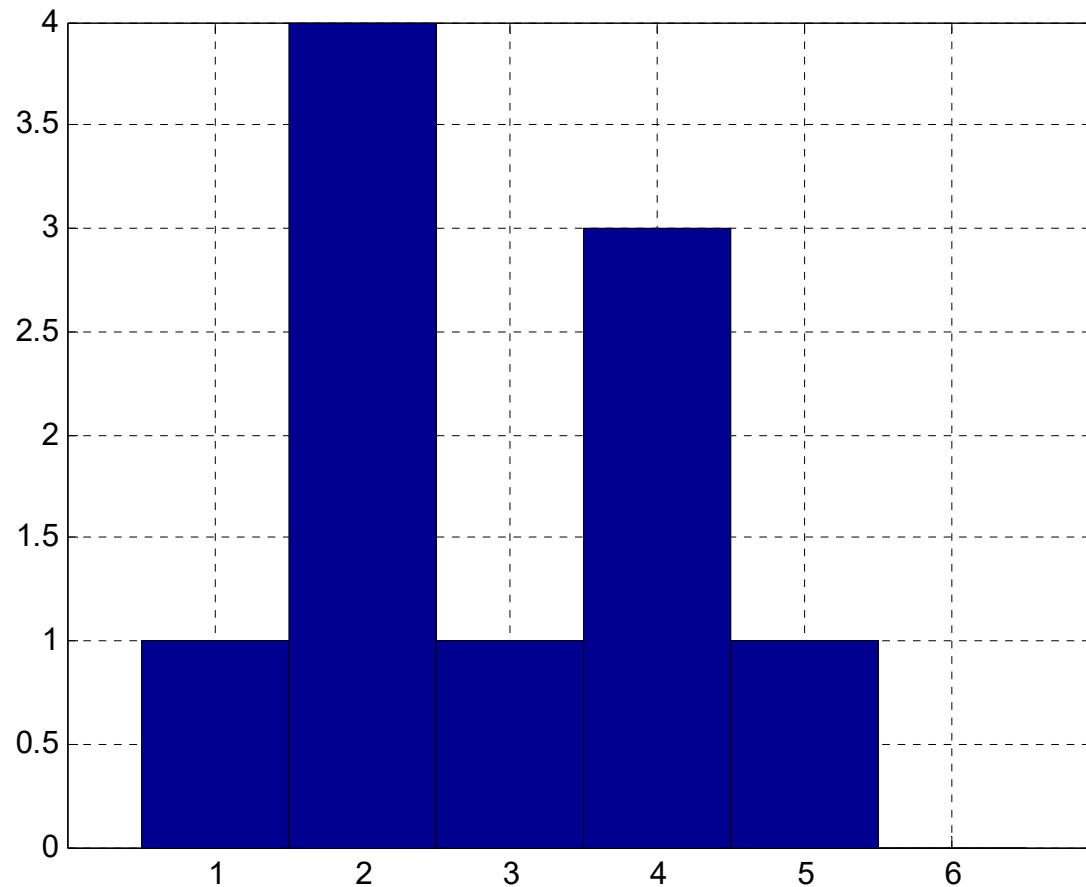
```
>> hist(x)
```



The width of each bin is $\frac{\text{max} - \text{min}}{10} = 0.4$

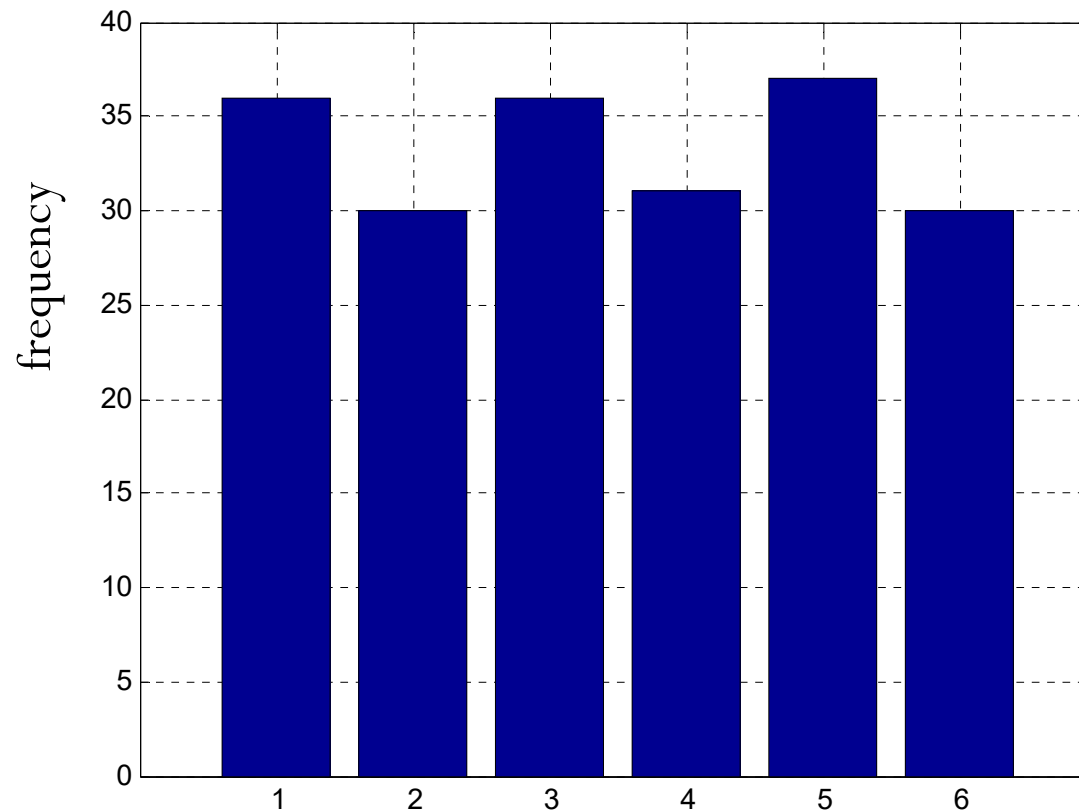
hist function: Example

```
>> X = randi(6,1,10)
X =
     4     2     4     5     2     1     2     2     3     4
>> hist(reshape(X,1,prod(size(X))),1:6)
>> grid on
```



$X \sim \text{Uniform}(\{1,2,\dots,6\})$

`X = randi(6,20,10)`



```
[N, x] = hist(reshape(X,1,prod(size(X))),1:6)
```

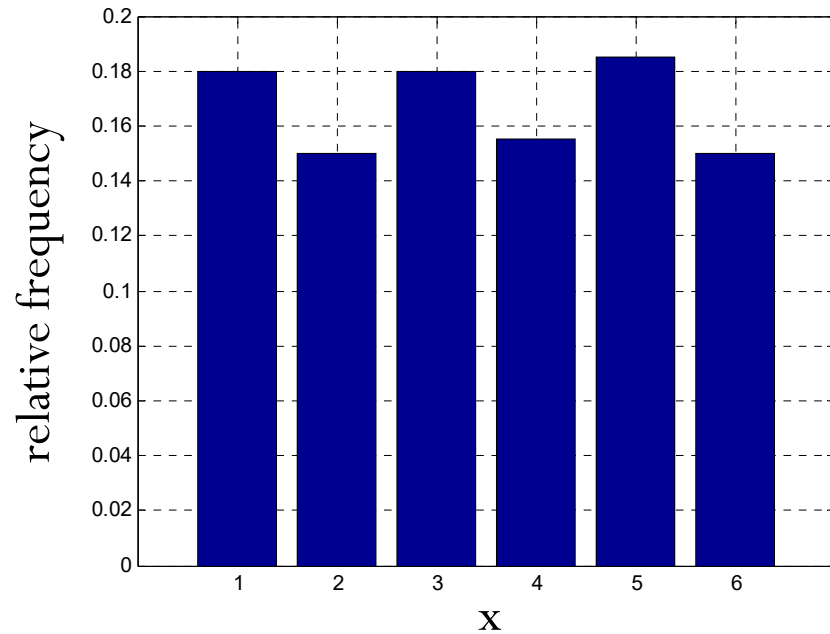
```
bar(x,N)
```

Grid on

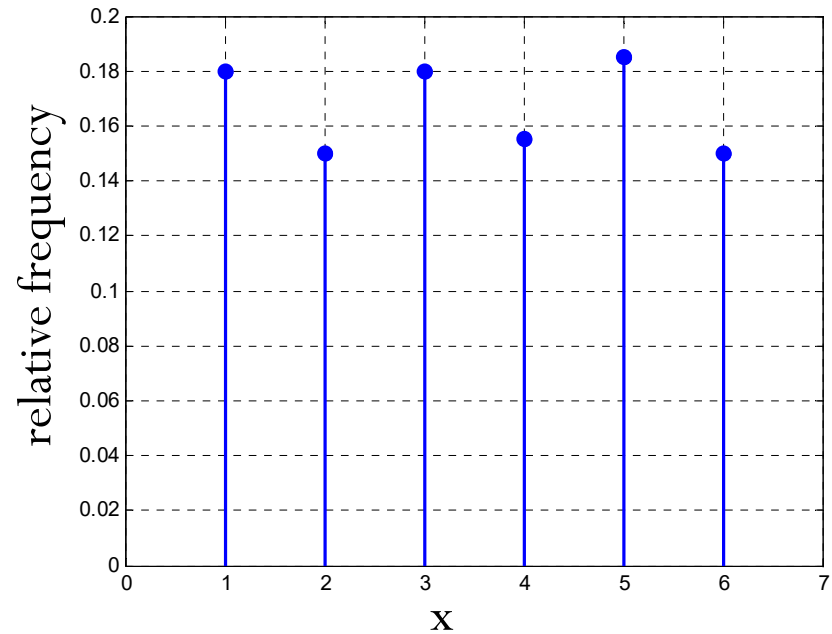
The `hist` command is used here for counting.

The “histogram” itself is drawn using the `bar` command.

Relative Frequency



```
rf = N/prod(size(X))  
bar(x,rf)  
grid on
```

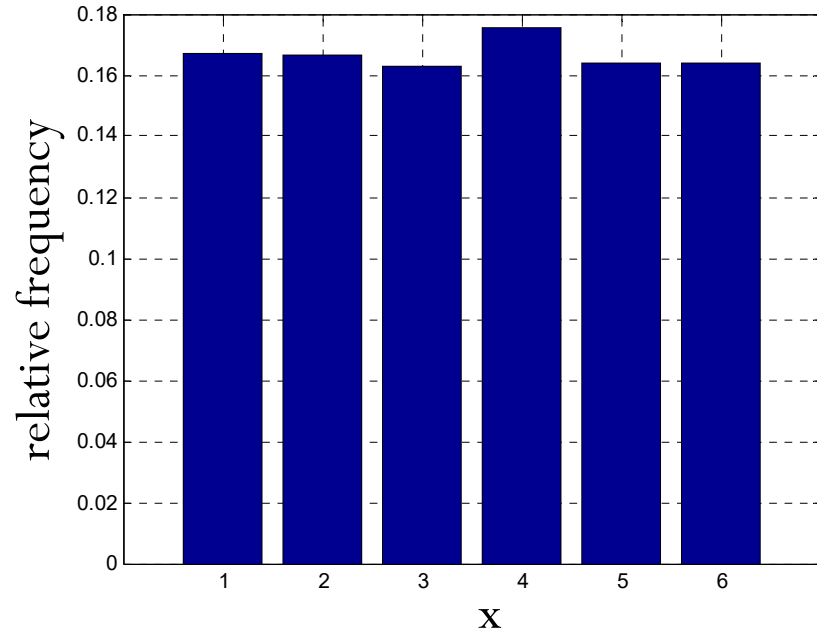


```
stem(x,rf,'filled','LineWidth',1.5)  
grid on
```

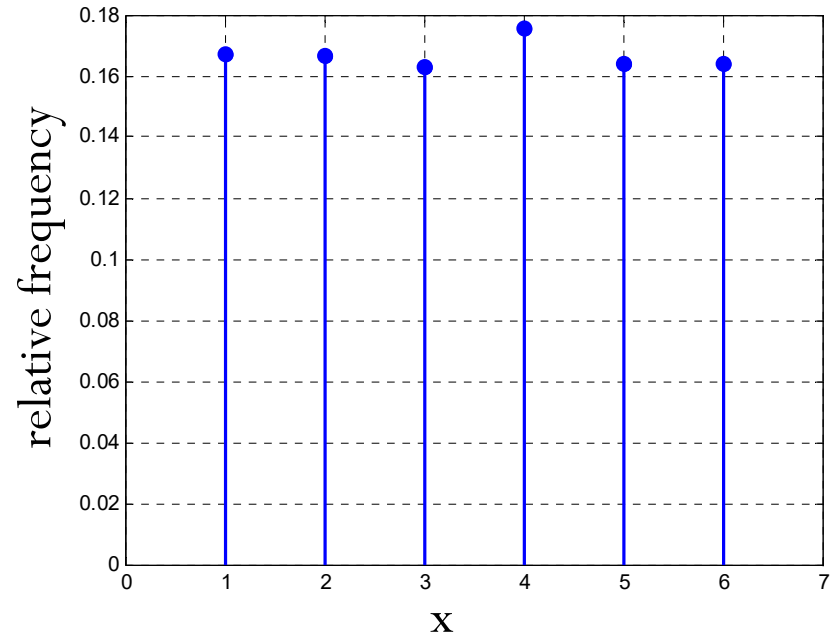
```
X = randi(6,20,10)
```



With larger number of samples



```
rf = N/prod(size(X))  
bar(x,rf)  
grid on
```



```
stem(x,rf,'filled','LineWidth',1.5)  
grid on
```

```
X = randi(6,100,100);
```



20-Sided Dice



Dice in Dungeons & Dragons

- A fantasy tabletop role-playing game (RPG)
- First published in 1974
- Widely regarded as the beginning of modern role-playing games and the role-playing game industry



D&D uses polyhedral dice to resolve random events. These are abbreviated by a 'd' followed by the number of sides. Shown counter-clockwise from the bottom are: d4, d6, d8, d10, d12 and d20 dice.

DUNGEONS DRAGONS



D20 Bowl Set



Flip an unfair coin 10 times. (The probability of getting heads for each time is 0.3.)

Count the number of heads.

$$X \sim \text{binomial}(10, 0.3)$$

```
>> X = binornd(10,0.3)
```

```
X =
```

```
3
```

Again, flip an unfair coin 10 times. Count #H.

```
>> X = binornd(10,0.3)
```

```
X =
```

```
2
```

Again, flip an unfair coin 10 times. Count #H.

```
>> X = binornd(10,0.3)
```

```
X =
```

```
2
```

Again, flip an unfair coin 10 times. Count #H.

```
>> X = binornd(10,0.3)
```

```
X =
```

```
5
```

Again, flip an unfair coin 10 times. Count #H.

```
>> X = binornd(10,0.3)
```

```
X =
```

```
1
```

Again, flip an unfair coin 10 times. Count #H.

```
>> X = binornd(10,0.3)
```

```
X =
```

```
4
```

```
>> X = binornd(10,0.3,20,10)
```

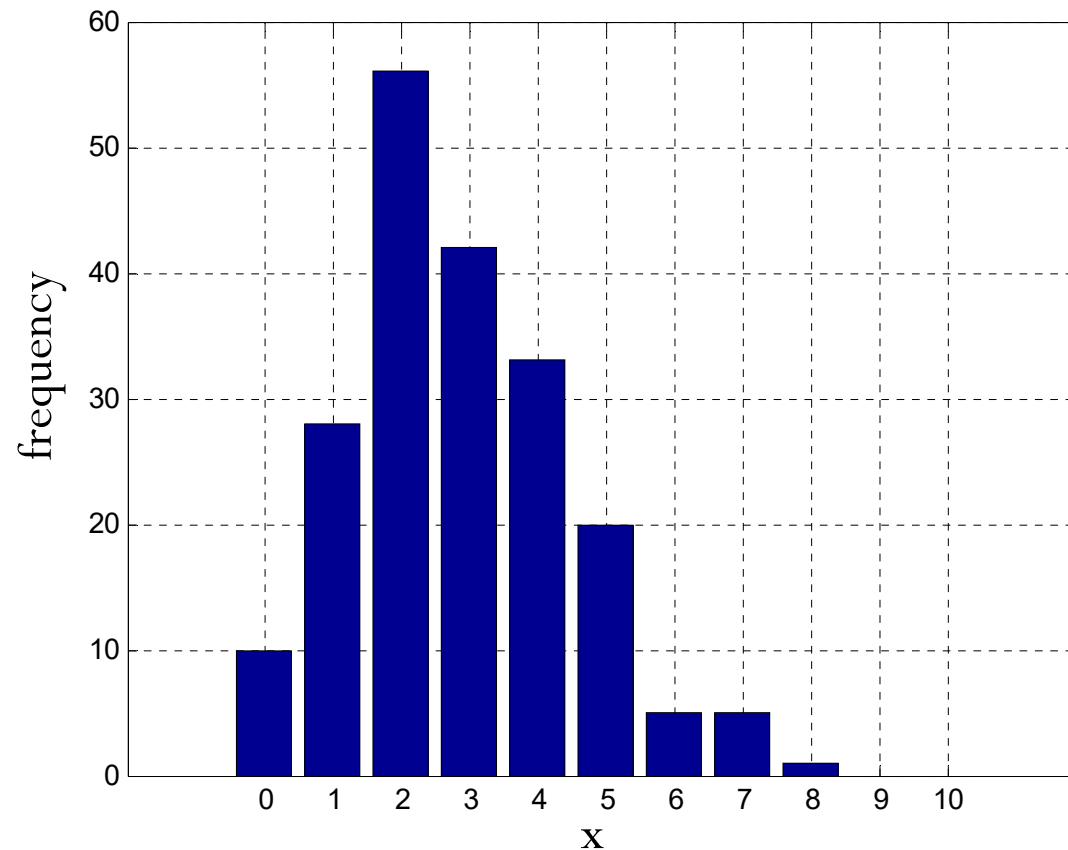
```
X =
```

3	4	4	5	7	2	2	2	2	1
3	5	3	1	0	4	2	1	2	3
5	2	2	6	4	2	2	4	3	1
1	2	2	4	2	4	3	3	3	5
4	1	4	3	3	4	2	2	2	2
2	1	3	1	5	2	5	2	1	2
4	0	3	3	2	1	2	1	3	1
4	4	0	2	3	6	2	3	1	1
5	0	3	3	7	1	3	1	3	8
1	2	4	4	1	5	2	4	5	1
5	2	4	6	3	2	3	3	5	0
2	4	0	0	2	2	3	2	0	2
4	3	3	2	2	2	1	2	7	4
2	4	2	1	3	3	4	3	5	2
5	3	2	3	4	2	3	3	1	2
2	6	2	3	4	4	4	5	6	7
5	1	2	4	3	3	0	5	0	2
1	4	1	3	1	4	2	4	2	4
5	2	2	3	3	5	3	5	2	1
4	2	4	3	2	5	7	2	3	1

Generate X 200 times. Put the results in a table of size 20×10



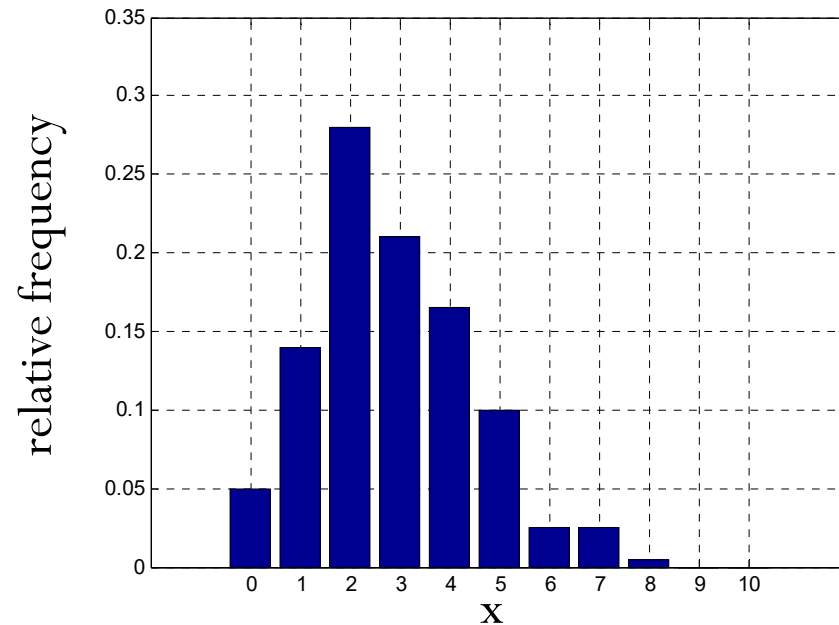
Histogram: $X \sim \text{binomial}(10, 0.3)$



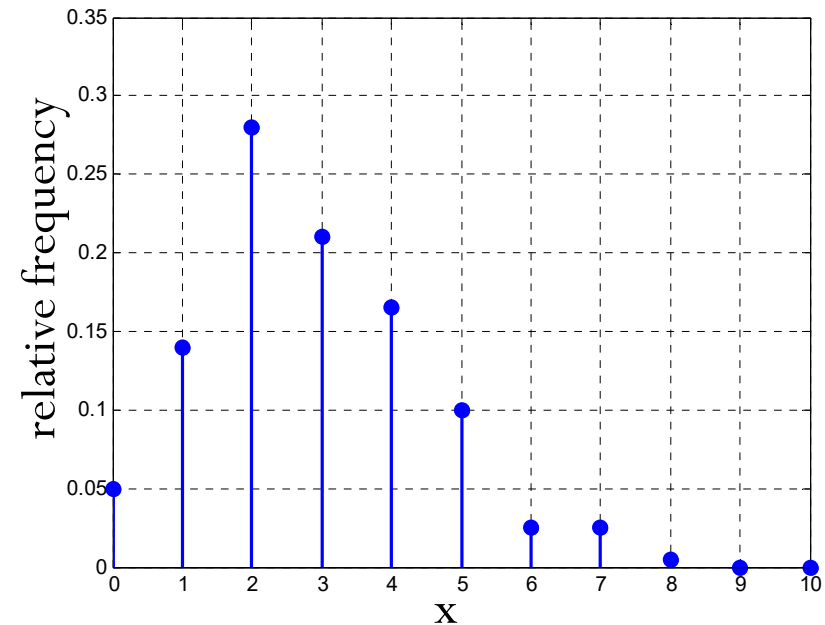
```
[N, x] = hist(reshape(X,1,prod(size(X))),0:10)
bar(x,N)
Grid on
```



Relative Freq.: $X \sim \text{binomial}(10, 0.3)$



```
rf = N/prod(size(X))  
bar(x,rf)  
grid on
```

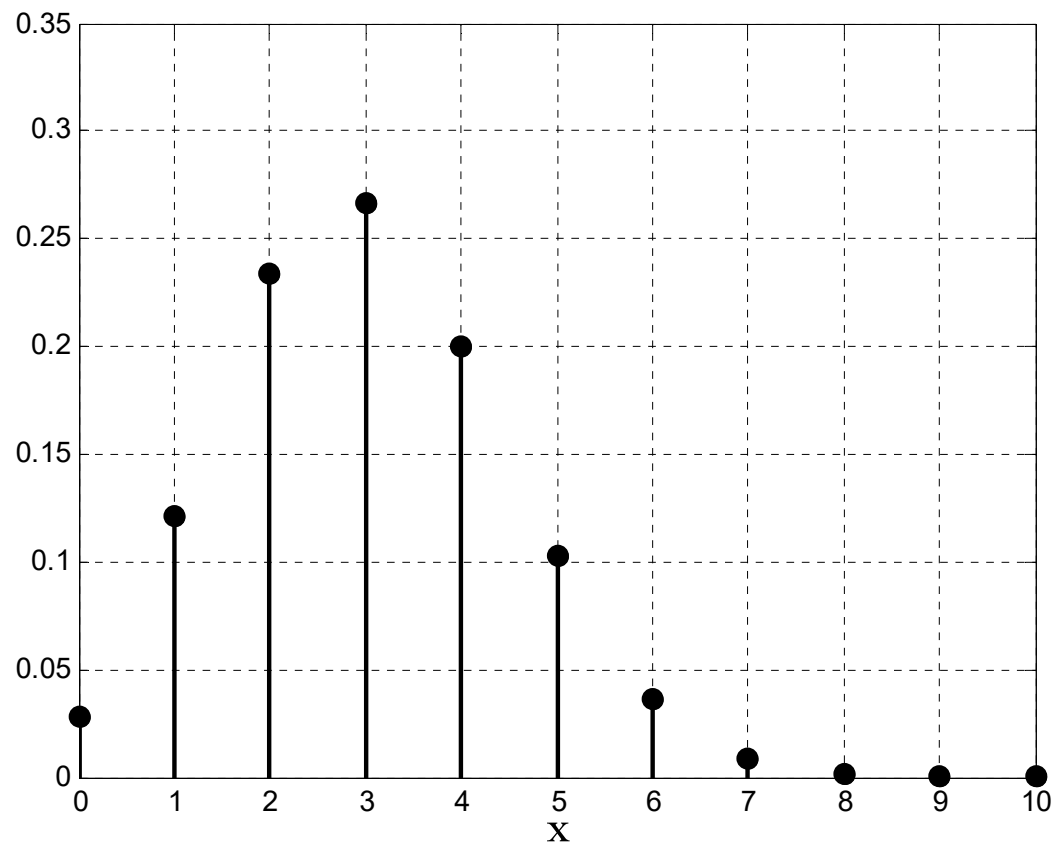


```
stem(x,rf,'filled','LineWidth',1.5)  
grid on
```



pmf for $X \sim \text{binomial}(10, 0.3)$

$$p_X(x) = \binom{10}{x} 0.3^x (1 - 0.3)^{10-x}$$



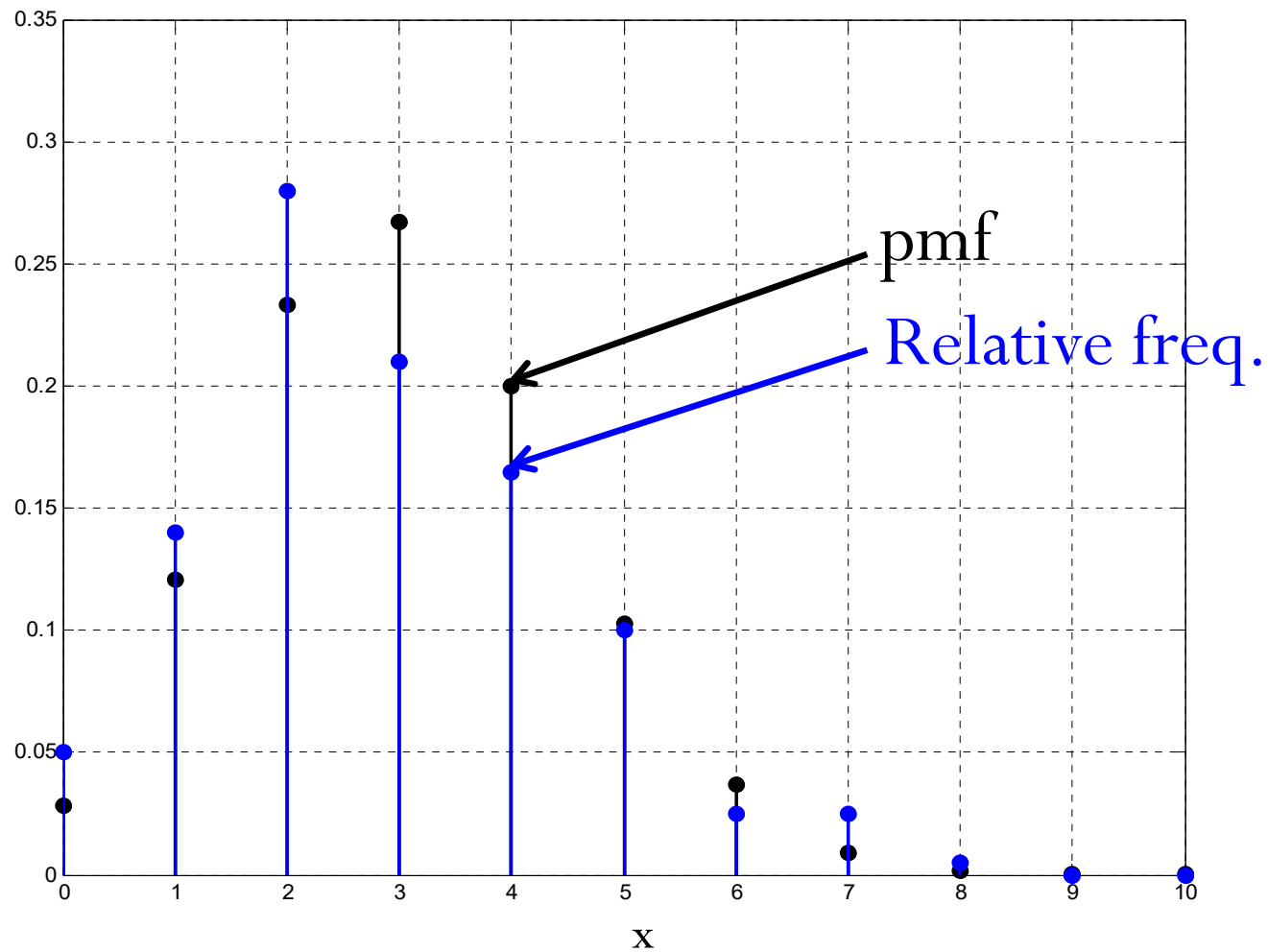
```
p = binopdf(x,10,0.3)
```

```
stem(x,p,'k','filled','LineWidth',1.5); grid on
```



$X \sim \text{binomial}(10, 0.3)$

```
X = binornd(10, 0.3, 20, 10);
```



$X \sim \text{binomial}(10, 0.3)$

```
X = binornd(10, 0.3, 100, 100);
```

